Value of travel time reliability: A review of current evidence

Carlos Carrion*, David Levinson

Department of Civil Engineering, University of Minnesota, 500 Pillsbury Drive SE, Minneapolis, MN 55455, USA

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A B S T R A C T

Travel time reliability is a fundamental factor in travel behavior. It represents the temporal uncertainty experienced by travelers in their movement between any two nodes in a network. The importance of the time reliability depends on the penalties incurred by the travelers. In road networks, travelers consider the existence of a trip travel time uncertainty in different choice situations (departure time, route, mode, and others). In this paper, a systematic review of the current state of research in travel time reliability, and more explicitly in the value of travel time reliability is presented. Moreover, a meta-analysis is performed in order to determine the reasons behind the discrepancy among the reliability estimates.

1. Introduction

Two of the most important values obtained from travel demand studies are the value of travel time (VOT), and the value of travel time reliability (VOR). The former links the monetary values travelers (or consumers) place on reducing their travel time (i.e. savings). The latter connects the monetary values travelers place on improving the predictability (i.e reducing the variability) of their travel time.

The concept of value of travel time has a long established history through the formulation of time allocation models from a consumer theory background. These models are reviewed thoroughly in Jara-Diaz (2007); a full chapter is dedicated to them. Also, the reader may refer to Small and Verhoef (2007) for a (succinct) review of the theory. In addition, more than a hundred of empirical estimates of the value of travel time has been carried out by both researchers and practitioners. Reviews such as Abrantes and Wardman (2011), Shires and de Jong (2009), Wardman (1998, 2001, 2004), Zamparini and Reggiani (2007b,a) serve as compilations of VOT estimates, and summaries of what has become mainstream knowledge in the field of travel demand. In contrast, the value of travel time reliability is a “newcomer” to this field, and although it has received increased attention, the procedures for quantifying it are still a topic of debate. The differences among studies span almost every aspect such as: experimental design (e.g. presentation of reliability to the public in stated preference [SP] investigations); theoretical framework (e.g. scheduling vs. centrality-dispersion); variability (unreliability) measures (e.g. interquartile range, standard deviation; a requirement in the centrality-dispersion framework); setting (or estimating) the preferred arrival time (e.g. assuming work start time as preferred arrival time in the scheduling approach); data source (e.g. revealed preference [RP] vs. state preference [SP]); and others. As a consequence, value of reliability estimates also exhibit a significant variation across studies.

In this paper, a systematic review of the theoretical and empirical research on travel time reliability is presented. Firstly, the concept of travel time reliability is discussed as it has become “defined” in the literature. Secondly, the most common theoretical models (scheduling and mean-variance [centrality-dispersion]) are described; others (e.g. mean-lateness) are
also briefly covered. Thirdly, the empirical evidence is compiled, and surveyed; the similarities and discrepancies of results across studies are discussed. Fourthly, a meta-analysis is performed to identify the sources of variations in travel time reliability estimates, and to provide an even more objective comparison of the reasons behind the estimates variability across studies. Lastly, the article is concluded.

2. Travel time reliability: concepts

The concept of travel time can be defined as the time elapsed when a traveler displaces between two (distinct) spatial positions. Certainly, this definition is applicable to any transportation mode (or combinations of them) regardless of the inherent differences across them. This is expected as travel time is typically understood as a one dimensional quantity (variable). Furthermore, travel time can be divided into several components depending on the analyst. For example, travel time of public transit modes tends to be split into waiting time, in-vehicle time, transfer time, and others.

In road networks, travel time may be split into two components: free flow time, and additional time. The former refers to the amount of time it takes a driver to arrive at his/hers destination without encountering any (or very little) traffic. The latter refers to each increase of travel time due to variations in the traffic conditions. These variations may be predictable (e.g. peak-hour congestion), or unpredictable (e.g vehicular crashes).

The predictable variations are events (i.e. traffic congestion) expected by travelers, and thus travelers (in principle) perform the necessary adjustments to offset the added costs (e.g. departing earlier to avoid arriving late at work). Such events (i.e. traffic congestion) are by itself a topic of interest to many researchers focusing on traffic flow theory (see Daganzo (2007) for an introduction to traffic flow theory). In transportation research, the morning peak-hour congestion is considered as a classic problem of trip scheduling under deterministic traffic conditions. Vickrey (1969) presented a solution to the problem with a single deterministic bottleneck model between an origin and destination, fixed and homogeneous travel demand, and endogenous departure time (i.e. trip scheduling choices). This model was further extended by Arnott et al. (1990), Laih (1994), Arnott et al. (1993), Arnott et al. (1994), Garcia (1999), Newell (1987), Daganzo and García (2000), Daganzo (1985), Daganzo (1995) and others. The interested reader on bottleneck theory, and its pricing applications may consult Yang and Huang (2005) and Small and Verhoef (2007).

The unpredictable variations are directly linked to the uncertainty of travel time. This uncertainty has been divided in three elements by Wong and Sussman (1973): variation between seasons and days of the week; variation by changes in travel conditions because of weather and crashes or incidents; and variations attributed to each traveler’s perception. Nicholson (1985), Daganzo (1995) and others. The interested reader on bottleneck theory, and its pricing applications may consult Yang and Huang (2005) and Small and Verhoef (2007).

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Travel time reliability is closely related to the unpredictable variations. This suggests that travelers choose under an uncertain environment as they may fail to predict their exact travel time before scheduling their trips (i.e. choosing a departure time). In the case of predictable variations, the travelers may adjust their departure time choice, and still be certain of arriving on time at their destinations. This is true even in a transportation system with high congestion. Notice that travelers are choosing under a certain environment. Therefore, it’ll be incorrect to consider predictable variations as examples of travel time (un)reliability (Bates et al., 2001). It should be noted that this travel time uncertainty may also extend to other choice dimensions (e.g. mode, route). Furthermore, the concept of travel time (un)reliability is defined as interchangeable with travel time variability (or unpredictable variation) in the transportation research literature; high variability means high unreliability, and vice versa. Consequently, it is natural to think of travel time in two dimensions: frequency, and magnitude. In other words, travel time defined as a distribution in the probability theory sense. In this way, travel time (un)reliability can be associated as a measure of spread to the travel time distribution. Distinct approaches have been proposed to model travel time reliability, and they are reviewed in the subsequent section. Moreover, similarities (i.e. travel time composed of deterministic and random elements) may be drawn to other transportation modes despite the fact that the concepts were mostly explained with a focus on road transportation.

3. Theoretical frameworks

3.1. Centrality-dispersion

The approach is mostly known in the context of risk-return models in finance. A decision-maker looks to maximize the option’s return while minimizing its associated risk. The option’s return is represented by the expected value, and the risk by the variance (see Markowitz (1999) for an overview). In a transportation context, the framework is based on the notion that not only travel time is a source of disutility, but also travel time variability (or unreliability). Thus, the formulation (with a linear-additive form) of the model, in a consumer theory background, is as follows:

\[ U = \gamma_1 \mu_T + \gamma_2 \sigma_T \]  

(1)

The traveler is minimizing the sum of the two terms (objective function for an unspecified choice dimension): the “expected” travel time of the trip, and the travel time variability of the trip. The “expected” travel time \( \mu_T \) is included...
as a centrality measure (e.g. mean) of the travel time distribution. The travel time variability ($\sigma_T$) is included as dispersion measure (e.g. standard deviation) of the travel time distribution. The $\gamma$ coefficients are exogenous parameters. Typically, the choice dimension is route choice, and the centrality (dispersion) measure is mean (variance or standard deviation) among studies using this approach. Mean-variance is also usual name the approach is known in the transportation literature, despite the fact that the centrality and dispersion measures vary among studies.

In the transportation literature, the framework was introduced by Jackson and Jucker (1982). Their original formulation is:

\[
\begin{align*}
\text{Minimize} & \quad E(T_p) + \lambda_k \text{Var}(T_p) \\
\text{subject to} & \quad p \in P_{AB} \\
& \quad \lambda_k > 0
\end{align*}
\]  

(2)

A traveler $k$ has a priori information of the mean ($E(T_p)$), and variance ($\text{Var}(T_p)$) of the travel time distribution for each route in their choice set ($P$) between an origin-destination pair ($AB$). $\lambda_k$ indicates the degree of risk aversion of the traveler $k$. The choice dimension is the route. Succinctly, a traveler $k$, with a degree of risk aversion $\lambda_k$, chooses the route that minimizes the objective function Eq. (2) given the expected and variance of the travel time distribution. The model proposed by Jackson and Jucker (1982) is usually estimated using discrete choice methods with the linear-additive specification given in Eq. (1). In this utility form plus a travel cost variable ($\gamma_3 C$), marginals rate of substitution may be computed to obtain important quantities such as the value of travel time (VOT), value of travel time reliability (VOR), and the reliability ratio (RR). These are defined formally in the previous order as,

\[
\begin{align*}
\text{VOT} &= \frac{\partial U}{\partial \mu_T} \\
\text{VOR} &= \frac{\partial U}{\partial \sigma_T} \\
\text{RR} &= \frac{\partial U}{\partial \mu_T} \frac{\text{VOR}}{\text{VOT}}
\end{align*}
\]  

(3) \quad (4) \quad (5)

In essence, this framework is based on expected utility theory developed by Von Neuman and Morgenstern (1944). The theory prescribes a set of axioms about how decision-makers deal with risky prospects (set of alternatives where a choice is selected) based on distinct states of nature (or states of the world). In simple words, there are several alternatives with several possible states of nature (the distribution of outcomes for each alternative), and associated to each combination of alternative and state of nature there is an outcome. In the transportation context, the set of alternatives could be routes, modes, schedules. The states of nature could be traffic signal failure, crashes, and others. The outcomes are likely to be the distribution of travel times for each alternative. In addition, the decision-maker ranks the risky prospects through the assumption of the existence of an ordinal utility function (i.e. $U = f(\text{outcome})$; the utility function associates a single real number to each outcome), and prefers the alternative with the highest expected utility ($E(U)$). Furthermore, an important feature of the expected utility framework is based on decision-making under risk. In other words, there’s a different between risk, where probabilities are known or at least knowable, and uncertainty, where probabilities are unknown. This difference may not be particularly useful for most practical purposes, or it may be irrelevant by considering subjective probability, and the axiomatic approach of expected utility theory (Takayama (1993) Chapter 5). Readers may also refer to Mas-Colell et al. (1995)Varian (1978), for treatments of expected utility theory.

The functional form of the utility function is not restricted by the axioms. In fact, the functional form chosen should be based on its close description of a decision-maker’s behavior. The functional form determines the risk preferences of the decision-maker. Functional forms may be selected based on regression analysis of experiments (e.g. gambling games that provide observations revealing the utility function) or computationally convenient forms (Hazell and Norton (1986) Chapter 5).

In the transportation literature, several functional forms have been considered to understand the risk behavior of travelers. Polak (1987) considered an alternative formulation to Jackson and Jucker (1982), where he defined the utility function of the traveler as a polynomial of second degree with respect to the travel time variable ($T$). Formally,

\[
U = \gamma_1 T + \gamma_2 T^2
\]  

(6)

This functional form Eq. (6) is known in the microeconomics literature (see Varian, 1978, Chapter 11, pp. 189) as equivalent to the mean-variance model under expected utility theory. This can be seen by applying the expectation operator to Eq. (6), and using a simple identity ($\text{Var}(X) = E(X^2) - (E(X))^2$),

\[
E(U) = \gamma_1 E(T) + \gamma_2 (E(T))^2 + \gamma_2 \text{Var}(T)
\]  

(7)

An important consideration is that the omission of the additional term [(E(T))^2] in Eq. (7) might bias the estimates of $\gamma_2$, especially when the formulation in Eq. (6) is accurate. In addition, the $\gamma_2$ indicates whether the traveler prefers alternatives (e.g. routes) with high variance of travel time (risk prone), low variance of travel time (risk averse) or only cares about the expected travel time (risk neutral). Furthermore, higher degrees of polynomials may be specified, and consequently in expected utility forms will lead to higher moments to be included. Another formulation proposed by Polak (1987) is
This functional form Eq. (8) is also known in the microeconomics literature (see Varian, 1978, Chapter 11, pp. 189–190); it describes a traveler with absolute risk aversion. Senna (1994) introduced a more general form based on the previous mentioned work, where the utility function is given by an algebraic term of degree $\beta$.

$$U = \gamma_1 T^\beta$$

The utility function can be written in terms of expected utility, by applying the expectation operator, and by considering some simple identities such as the definition of covariance, in the following form:

$$E(U) = \gamma_1 \left(E\left(T^2\right)\right)^2 + \gamma_1 \text{Var}(T^2)$$

The Eq. (10) exhibits certain properties. The $\beta$ parameter estimates the degree of risk aversion/proneness by the travelers. Another important property is that the value of time and the value of variability (reliability) depend directly on the travel time distribution. The reader should refer to appendix 2 in Senna (1994) for the mathematical proofs.

It should be noted that all the previous $\gamma$ coefficients are parameters to be estimated, and expected to be negative.

### 3.2. Scheduling delays

Historically, this approach has been linked to the departure time choice (or trip scheduling) studies. The basis for the approach rests on the time constraints (e.g. work start time) a traveler may face, and thus it associated costs due to early or late arrival. This leads to the idea of a traveler intrinsic choice of a preferred arrival time (PAT); the point of reference that delimits whether an arrival is early or late. Gaver (1968) is one of its earliest proponents. He introduced a theoretical framework for describing variability in trip-scheduling decisions. He considered distinct head start strategies for given delay distributions along with the costs of arriving early or late. In addition, statistical estimation procedures (non-parametric and parametric) are provided to estimate the probability density distribution of the trip delay, when it is unknown to the researcher. Vickrey (1969), as described previously, also considered the trade off travelers face between queue delay, and schedule delay of arriving early or late at work. Furthermore, a similar hypothesis is the existence of a “safety margin” advocated by Knight (1974) and Pells (1987). Knight (1974) suggested that travelers consider a slack time (i.e. safety margin) between their (average) arrival time and their own work start time. This safety margin allows the reduction of the probability of late arrivals, and implies that travelers have a preference of arriving early to work (i.e. existence of positive utility for the time spent at work before work start time). In essence, Knight (1974) hypothesizes that the departure time chosen happens when the marginal utility of time spent at home is equal to the marginal utility of arriving early to work plus the marginal utility of arriving late to work. Pells (1987) further argued that two opposite existing factors are at play: the need to minimize the frequency of late arrivals, and maximize the time spent at home relative to the early time spent at work. Travelers meet the first factor by allocating a safety margin, and they meet the second factor by maintaining the safety margin at required levels (i.e. safety margins are acceptable when there’s more time spent at home relative to early time spent at work).

Another important contribution is by Small (1982), based on some of the previous articles (mostly Gaver (1968) and Vickrey (1969)). He formulates a theoretical model based on the traditional utility maximization framework (i.e. consumer behavior; see Varian, 1978) with insights from time allocation models (e.g. Becker (1965), DeSerpa (1971), Bruzelius (1979)). Small (1982)’s model consists of tying explicitly the departure time choice, and also adding a workplace constraint (i.e. an equation linking departure time, and working hours with merits or penalties to the wage rate; workplace policies where pay is docked by tardiness or bonuses are given for arrival on time) to the utility function of a traveler. In this way, the traveler’s utility is influenced by the departure time, and also the value of time is influenced by the workplace constraint. Properties of this formulation may be reviewed in Jara-Diaz (2007, Chapter 2, pp. 67–69), and Carrion (2010, Chapter 2, pp. 11–15). Furthermore, he specifies a functional form for the (indirect) utility of scheduling:

$$U(t_d, PAT) = \gamma_1 T + \gamma_2 \text{SDE} + \gamma_3 \text{SDL} + \gamma_4 \text{DL}$$

This is a linear-additive form, where the $\gamma$ coefficients are parameters to be estimated, and expected to be negative. In this equation, the travel time ($T$) is not only included but also the scheduling delays which are divided by early (SDE; defined as Max(0, PAT – $T + t_d$)) and late (SDL; defined as Max(0, [T + $t_d$] − PAT)) arrivals according to a preferred arrival time (PAT), and a binary term DL to indicate whether it is a late arrival or not (SDL > 0). The SDE, SDL and DL terms represent scheduling considerations for the workplace constraint. $t_d$ is the decision variable (usually a continuous real variable for mathematical models), and it represents the traveler’s departure time choice. Up until this point, the scheduling delay framework describes travelers’ choices under certainty. Moreover, Bates et al. (2001) points out that capacity restrictions (i.e. $t_d$ is no longer independent of $T$; travelers cannot choose the same $t_d$ as queueing is now present) of the transportation facility readily translates this framework to one extensively studied using bottleneck models (e.g. Arnott et al. (1990), Laih (1994), Arnott et al. (1993), Arnott et al. (1994)). This implies (as discussed in Section 2) the decomposition of travel time into: free flow travel time, and additional travel time due to recurrent congestion.
The model proposed by Small (1982) is usually estimated using discrete choice methods (i.e. the departure times are discrete intervals if scheduling is the choice situation) with the linear-additive specification given in Eq. (11). In this utility form plus a travel cost variable \( \gamma_C \), marginals rate of substitution may be computed to obtain important quantities such as the value of travel time (VOT), value of scheduling delay early (VSDE), and the value of scheduling delay late (VSDL). Researchers often discard the lateness penalty variable (DL), because it adds a discontinuity that is inconvenient to mathematical optimization models (gradient-based), and a missing lateness penalty may translate into a higher lateness scheduling delay in econometric models. These are defined formally in the previous order as,

\[
\begin{align*}
VOT &= \frac{\partial U}{\partial T} \\
VSDE &= \frac{\partial U}{\partial SDE} \\
VSDL &= \frac{\partial U}{\partial SDL}
\end{align*}
\]

**3.2.1. Scheduling delays + dispersion**

In Noland and Small (1995), the previous scheduling approach is extended to include explicitly the uncertainty of travel time (i.e. unpredictable variation; see Section 2). This uncertainty is expressed in the form of a random variable \( T_d \), preserving Noland and Small (1995) notation) with a given probability density function, and with the restriction of being greater or equal to zero.

\[
E(U(t_d)) = \int_0^\infty U(t_d)f(T_d)dT_d = \gamma_1 E(T) + \gamma_2 E(SDE) + \gamma_3 E(SDL) + \gamma_4 P_L
\]

The objective function of the traveler changes (also the utility function is traded for a trip cost form in Noland and Small (1995), but we choose to keep it for coherency), and now the consumer maximizes the expected utility \( E(U(t_d)) \) by choosing the optimal \( t_d \) (see Eq. (15)) for a given probability density function of \( T_d \). The elements of Eq. (15) include the scheduling costs for early (SDE) vs. late (SDL) arrival at work presented earlier (see Eq. (11)), but also the last term employs the distribution of the random variable \( T_d \) in order to compute the probability of being late. \( P_L \) is simply \( E(DL) \) (note DL is an indicator function) conditional on \( t_d \). Therefore, the last term \( P_L \) also contains the costs of travel time unreliability as the dispersion (or variability) of the travel time distribution affects the calculated probabilities. In addition, travel time dispersion (or variability) may increase the propensity of early arrivals, and thus high earliness costs can be incurred. This implies variability and scheduling costs are related. In fact, Bates et al. (2001) argues that \( \gamma_2 E(SDE) + \gamma_3 E(SDL) \) may approximate the \( \gamma_2 \sigma T \) in the centrality-dispersion model (see Section 3.1) under certain conditions: travel time distribution is independent of departure time; \( \gamma_4 = 0 \) in Eq. (15) or no lateness penalty; departure time is continuous; congestion dynamics are neglected as in travel time is independent of departure time. Such mathematical properties and others are discussed in detail in Bates et al. (2001).

Recent work by Fosgereau and Karlstrom (2010) proved mathematically the previous statement by Bates et al. (2001) (scheduling models approximated by mean-variance models). They indicate this can be achieved with knowledge not only of the estimated parameters \( \gamma_1 \) and \( \gamma_2 \) in Eq. (11) for the expected travel time and variance, but also the travel time distribution, and the optimal probability of being late. This proof follows the assumptions presented earlier by Bates et al. (2001), and also the obvious assumptions the mean of random variable \( T_d \); they actually use a standardized form with mean 0 and variance 1 is defined (i.e. exists), and that it has an invertible distribution. These assumptions are more general than the previous ones of assuming the density function of the random variable \( T_d \) follows an uniform or exponential distribution (see Bates et al., 2001; Polak, 1996; Noland and Small, 1995; Small and Verhoef, 2007). The interested reader should refer directly to Fosgereau and Karlstrom (2010), especially appendix A for more details. An empirical verification is also included in the paper.

It should be noted that all the previous \( \gamma \) coefficients are parameters to be estimated, and expected to be negative.

Other recent work has followed different paths: inclusion of risk attitudes in scheduling models (Senbil and Kitamura, 2004; Michea and Polak, 2006; Schwanen and Ettema, 2009; Li et al., 2010); alternative formulation of schedule early (SDE), and schedule late (SDL) (Tilahun and Levinson, 2010); and scheduling preferences with non-constant marginal utilities or time-varying parameters (Tseng and Verhoef (2008) and Fosgereau and Engelson (2011) and Jenelius et al. (2011)).

In Li et al. (2010), a non-linear utility specification (they assume a utility function of the form \( U = \gamma_1 x^{\gamma_2} \), where \( x \) is any variable in the model and \( x \) represents risk attitude) is used like in the other mentioned studies (e.g. Michea and Polak (2006)), but the parameter \( x \) representing risk attitude (\( x \)) was assumed random, and thus the parameters of its population density function can be estimated using a mixed logit formulation. The idea of risk attitudes has been considered before in microeconomics, and discussed implicitly in Section 3.1.

Tilahun and Levinson (2010) introduces a new approach for measuring SDE and SDL in Eq. (11) consisting of two moments: the first representing on average how early the traveler has arrived by using that route; and the second representing on average how late that individual arrived by using that particular route. They assume that the deviation of the two moments (average late or average early) from the most frequent experience is a representative way of getting together the possible range and frequencies experienced by the travelers. Thus, this measure may considers scheduling constraints as well, albeit not separately from (un)reliability of travel time.
The scheduling preferences models (Tseng and Verhoef (2008) and Fosgereau and Engelson (2011) and Jenelius et al. (2011)) generalize Small (1982) by assuming the $\gamma$ parameters (except for the binary lateness penalty, which is discarded) in Eq. (11) are time-dependent (earliness and lateness penalties vary by time of day). Tseng and Verhoef (2008) introduced the formulation based on Vickrey (1973). Fosgereau and Engelson (2011) extended the formulation to account for random travel times. Jenelius et al. (2011) considered chained trips, and thus more than one activity. In addition, Jenelius (2011) extends his previous chained trip formulation to consider random travel times.

3.3. Mean-lateness

This approach is widely used in passenger rail in the UK, and it was proposed by the Association of Train Operating Companies (ATOC, n.d.). It consists of two elements under the expected utility paradigm: schedule journey time ($\text{Sched}$), and the mean lateness at destination ($L$). The former refers to the travel time between the actual departure time and the scheduled arrival time, and the latter refers to the mean of the lateness. The lateness is defined as the time between scheduled departure and actual departure (lateness at boarding), and time between scheduled arrival and actual arrival (lateness at destination). In the original ATOC formulation (see Eq. 16) only the mean (positive [$L^+$]; negative values meaning early arrivals are not considered) lateness at destination is considered, but this is expanded (see Eq. (17)) in Batley and Ibanez (2009) to include the lateness at boarding (positive [$B^+$]; negative values meaning early departures are not considered) as well, plus the train fare is added to calculate marginal rates of substitution between temporal quantities and travel cost (e.g. value of time [VOT]). It should be noted that Batley and Ibanez (2009) also tested the inclusion of another variable ($\gamma_5 \sigma_T$) representing the standard deviation of the in-vehicle journey time.

$$E(U) = \gamma_1 \text{Sched}T + \gamma_2 L^+$$

$$E(U) = \gamma_1 \text{Sched}T + \gamma_2 L^+ + \gamma_3 B^+ + \gamma_4 C$$

It should be noted that all the previous $\gamma$ coefficients are parameters to be estimated, and expected to be negative.

4. Empirical evidence

Most of the initial research hinting towards travel time reliability (or predictability) was based on questionnaires ascertaining travelers’ preferences, and thus it was mainly qualitative. For example, Vaziri and Lam (1983) asked commuters to list and rank possible reasons affecting their route choice, and also write others that were not listed. The results (directly) related to reliability were: “it has fewer accidents or unexpected toe-ups” (ranked fourth); and “it has smaller variation in trip times” (ranked eight). Also Chang and Stopher (1981), indicated similar results (important of factors related to reliability) with travel mode preferences. Furthermore, Prashker (1979) was the first to explicitly account for reliability; he included different levels of variation for variables such as in-vehicle travel time, parking search time, and bus waiting time. Moreover, the research has since moved to a quantitative state. Empirical estimates have been obtained based on statistical models (typically using discrete choice methods) of the previous theoretical frameworks. The data sources for statistical modeling are usually from: stated choice experiments (i.e. stated preference) with a variety of presentations for questionnaires; and revealed choices (i.e. revealed preference) with objective travel time distributions (i.e. travel times measured by Global Positioning System [GPS] devices, loop detectors, and others). Both data sources may be combined as well to overcome some of their own deficiencies (see Louvierie et al., 2000). Revealed choices may be estimated using subjective travel time distributions (i.e. travel times reported by travelers memory), but this has not be done yet. The differences between subjective travel time distributions and objective travel time distributions are likely to be based on perception errors. This discussion is summarized in Fig. 1. These reliability issues are discussed further subsequently.

Fig. 1. Data sources for value of travel time reliability studies.
4.1. Stated preference studies

Most of the estimates of valuation of reliability have been obtained through stated choice experiments. In fact, Bates et al. (2001) argued that (at the time of publication) there were no adequate real examples at the level of detail required for ascertaining reliability estimates using revealed preference data (RP). Thus, they considered stated preference as the best bet, which had dominated completely the empirical studies (and its estimates) so far. However, they admitted that survey design (i.e. presentation of questions) may affect the outcome of the reliability estimates. This is likely as travel time reliability is difficult to present to subjects without any statistical background unlike travel time savings.

Early studies focused on paired comparison questions of hypothetical route alternatives. A pair was typically formed of two "usual" times and corresponding delays to one alternative of the pair. The delay was always given to the shortest "usual" time of the pair. In this way, variability measures were incorporated for the estimation of the models. Jackson and Jucker (1982) introduced the mean-variance approach (or centrality-dispersion framework covered in Section 3.1) in order to quantify the effects of travel time (un)reliability on route choices. The analysis of the subject’s stated preference was done by optimizing an objective function (a linear programming problem) in which the expectation and variance of the travel times are variables. This method also allowed for the estimation of a degree of risk aversion parameter for the subjects. Jackson and Jucker (1982) found that some commuters prefer the more reliable route, even if the expected travel time is higher in comparison to other routes with shorter expected travel time, and higher uncertainty. This result agrees with the notion of a distribution of the degrees of risk aversion in the subjects. Abdel-Atty et al. (1997) used two stated preference techniques (a computer aided telephone interview and a mail-back survey) in order to investigate the effect of travel time reliability and traffic information on commuters. The first survey consisted of offering five options, each with two routes with distinct travel times (one with the same travel time for every day, and the other with different travel times on some days) for the travelers to choose, and the second one consisted of two routes (one presumably familiar to the subjects) with similar travel time variation scheme to the previous survey, but also included a section with traffic information. The analysis of the survey data was done with binary logit models including variables such as standard deviation, mean and gender. They found that commuters consider reliability characteristics in their route choice preference, and pay attention to travel information enough to be influenced in some scenarios to deviate from their usual routines. Another finding was that males tend to choose the uncertain route more than females, and thus indicating a difference in risk attitudes related to gender.

Black and Towriss (1993) developed a different approach to the previous researchers. The approach focused more on presenting the same mean travel time for each route (i.e. alternative), but with distinct variability as it was presented with several possible travel times. In essence, the survey respondents choose between distinct options with a varying spread of travel times, mean travel times, and travel cost. Moreover, they specified and estimated linear utility function following the mean-variance approach. Their results indicated that travel time variability was a significant factor, although the magnitude was less compared to the mean travel time. In addition, they introduced the concept of reliability ratio as defined in Eq. (5). Small et al. (1999) also investigated the effects of reliability and scheduling based on Black and Towriss (1993)’s question format with minor modifications. Two alternative choices with mean travel times, a distribution of five arrival times with respect to an implied preferred arrival time, and a travel cost. Small et al. (1999) used the collected survey data to estimate mean-variance models, scheduling models, and combining both approaches (adding terms of both Eqs. 1 and 15 plus a travel cost term \( \gamma_6C \)): \( U = \gamma_1M + \gamma_2C + \gamma_3SDE + \gamma_4SDL + \gamma_5DL + \gamma_6C \) in econometric models using discrete choice methods (consistent with Random Utility models). Small et al. (1999) also further included observed heterogeneity factors interacted with travel time (mean) and travel time variability (standard deviation) variables such as: income, number of adults, number of children, and trip purpose (work trip or non-work trip). They found that survey respondents with children have a higher disutility associated with lateness compared to those without children, and also lower income respondents incur less disutility in early arrivals compared to other respondents with higher income levels. Also Koskenoja (1996), Small et al. (1995) did an extensive exploration of the relationship between travelers occupations and other socio-demographic variables, and their preferences toward travel time reliability. Her results show differences such high income commuters with young children preferring not to increase commute time to decreased expected early arrival penalties. On the other hand, low income commuters are willing to trade 0.6 minutes of commute time to decrease 1 minute of expected early arrival penalties. In addition, Small et al. (1999) found that combining terms of the mean-variance and scheduling models lead to statistically not significant estimate of the travel time variability measure (standard deviation in this case; \( \gamma_6 \) is found statistically not significant from zero). This is expected as it was discussed that the mean-variance and the scheduling approaches are equivalent under certain conditions (see Section 3.2.1). Furthermore, they found that non-linearities are present in the scheduling model. This is verified by adding a quadratic term of earliness penalty \( (\gamma_6SDE^2) \) that is found statistically significant different from zero. This quadratic term implies that positive utility (Knight (1974) argued in favor of such existence; see Section 3.2) exists up until a point of about three minutes. In addition, the non-linearities results indicate that the penalties (early or late) are present and are related to the preferred arrival time. Koskenoja (1996), Small et al. (1995) also explored non-linearities in mean travel times, and early penalties using quadratic terms similar to Small et al. (1999). The scheduling preferences models (Fosgereau and Engelson (2011), Jenelius et al. (2011), Jenelius (2011), Tseng and Verhoef (2008); see Section 3.2.1) hypothesize that the scheduling terms \( (\gamma_3SDE + \gamma_4SDL) \); they discard DL because of its discrete nature) are actually functions that depend on the time of day. In fact, Tseng and Verhoef (2008) tested using stated preference data that the value of travel time is different across time of day. Liu et al. (2007) also indicated the non-constancy of the value of travel time, and value of reli-
et al. (1999). The first questionnaire contains three sections: average travel time experience, probability of time of arrival, and trip costs. The first section presents a division of average travel time very similar to Hensher (2001). The second section presents the arrival time with respect to a implied preferred arrival time very similar to Small et al. (1999) distribution of histograms), mode-right range (100th percentile–50th percentile), and introduce a new measure consisting of two moments (one representing earliness, and another lateness), Tilahun and Levinson (2010) found a reliability ratio of 0.89 for the mode-variability model. They also found that survey respondents value lateness (in their proposed measure) similarly to travel time reliability. Also, the uncertainty component is actually more closely related to the schedule delays (allocated extra time to avoid arriving late) rather than measures of the travel time variability (e.g. standard deviation). Hollander (2006)’s survey design consists of a histogram for each alternative in a pair. They also introduce an education phase to explain to survey respondents what the histograms convey. They test a mode-variance model (mode is the most frequent travel time shown in the histograms), mode-right range (100th percentile–50th percentile), and introduce a new measure consisting of two moments (one representing earliness, and another lateness), Tilahun and Levinson (2010) found a reliability ratio of 0.89 for the mode-variability model. They also found that survey respondents value lateness (in their proposed measure) similarly to travel time savings. Li et al. (2010) introduce two distinct questionnaires representing variability based on Hensher (2001) and Small et al. (1999). The first questionnaire contains three sections: average travel time experience, probability of time of arrival, and trip costs. The first section presents a division of average travel time very similar to Hensher (2001). The second section presents the arrival time with respect to a implied preferred arrival time very similar to Small et al. (1999) distribution of arrivals. The third section includes travel costs; a running cost is presented in addition to tolls costs. The second questionnaire is similar to the first questionnaire, except that the sections are not divided, and the distribution of arrival times is replaced with a row indicating the trip time variability (i.e. amount of minutes plus or less with respect to the travel time). Travel costs are presented as taxi fares, and toll costs. Li et al. (2010) tested the questionnaires with commuters and non-commuters, and found that non-commuters values less travel time savings, lateness penalties, and travel time reliability relative to commuters. The non-commuters’ reliability ratio is higher compared to commuters. In addition, Li et al. (2010) argued that the survey design similar to Small et al. (1999)’s first questionnaire is better understood by survey respondents in comparison to the survey design similar to Jackson and Jucker (1982)’s second questionnaire. It should be noted that there are differences between Li et al. (2010)’s second questionnaire and Jackson and Jucker (1982)’s questionnaire even though Li et al. (2010) considers them as similar. An important difference is that Jackson and Jucker (1982) presents variability as number of additional minutes of delay per week, and Li et al. (2010) presents delays by plus or less minutes with respect to the travel time.

An important contribution to the design of stated preference surveys for analyzing travel time variability is Tseng et al. (2009). They use face-to-face interviews to investigate the understanding of subjects with most of the previously discussed questionnaires (Bates et al. (2001), Copley et al. (2002), Hollander (2006), Small et al. (1999)). The analysis consisted of questions about the respondents subjective preferences with regards to the formats, and questions that tested for consistency using loop detector data. Therefore, it can be argued that non-linearities are starting to be considered in the recent mathematical models of scheduling preferences.

In the late 1990s and 2000s, the stated preference research focused on designing better presentations of questions about variability. Cook et al. (1999) and Bates et al. (2001) asserted that the presentation of variability in the questions has a significant impact in the estimates, because of a mismatch between the respondents and analysts understanding of the abstract situation. Thus, analysts must validate the understanding of their questionnaires with the survey respondents. Bates et al. (2001) and Cook et al. (1999) verified the understanding of respondents by presenting closely matching pairs of questions. They found that about 90% of respondents correctly identified the differences in the questions, except in cases where zero delay was included, and respondents will choose the more variable (less reliable) alternative of the pair. Bates et al. (2001) and Cook et al. (1999) proposed an alternative design for the presentation of variability. This design consists of circular arrangement of arrival times with respect to a given preferred arrival time. Each arrival time is represented by a box indicating how many minutes early or late the respondent will arrive. Bates et al. (2001) and Cook et al. (1999) included education phases to increase the likelihood of survey respondents understanding of their circular presentation. Copley et al. (2002) studied different presentations (linear arrangements of possible travel times, circular arrangements of possible travel times, and histogram representation of possible travel times) of travel time variability. A qualitative approach by interviewing respondents suggested a preference for linear arrangements and histograms presentations of variability. Copley et al. (2002) prefer the histogram representation, because it can present a large volume of information, and their qualitative research showed that it was understood with little effort.

Other researchers also tried alternative presentations. Hensher (2001) used bar diagrams dividing the total travel time into: free flow, slowed down, stop/start, and uncertainty. The bars also provided numbers for the amount of minutes of each component of the total travel time for pairs of alternatives. The alternatives also included a travel cost component in order to calculate trade offs between cost and the distinct components of time. It should be noted that Hensher (2001) was more concerned with investigating the values that travelers assign to the distinct components of the total travel time rather than travel time reliability. Also, the uncertainty component is actually more closely related to the schedule delays (allocated extra time to avoid arriving late) rather than measures of the travel time variability (e.g. standard deviation). Hollander (2006) uses a very different presentation compared to the previous discussed researchers. Hollander (2006)’s survey design consists of five bars per alternative indicating the time of departure (e.g. 8:15) on the top of the bar, and the time of arrival at the bottom of the bar (e.g. 8:30). In this way, travel times are not given in terms of minutes explicitly. In addition, travelers are told the time they should be at their destinations, explicitly. Hollander (2006) estimated a scheduling model, and a mean-variance model. The results indicate that the reliability ratio was very low 0.1 (this is significantly small compared to most studies) in the mean-variance model, and most users were willing to pay more to avoid arriving late in the scheduling model. Asensio and Matas (2008) uses a similar presentation of variability as Small et al. (1999) (average travel time, and a distribution of possible travel times). Asensio and Matas (2008) also tests scheduling and mean-variance models. They find that the inclusion of the variability measure plus scheduling delay measures resulted in lost of statistical significance in the reliability variables of both models with the exception of schedule delay late. Thus, indicating a correlation between both approaches as theoretically expected, and already discussed. Tilahun and Levinson (2010) introduces a variability format consisting of a histogram for each alternative in a pair. They also introduce an education phase to explain to survey respondents what the histograms convey. They test a mode-variance model (mode is the most frequent travel time shown in the histograms), mode-right range (100th percentile–50th percentile), and introduce a new measure consisting of two moments (one representing earliness, and another lateness), Tilahun and Levinson (2010) found a reliability ratio of 0.89 for the mode-variability model. They also found that survey respondents value lateness (in their proposed measure) similarly to travel time savings. Li et al. (2010) introduce two distinct questionnaires representing variability based on Hensher (2001) and Small et al. (1999). The first questionnaire contains three sections: average travel time experience, probability of time of arrival, and trip costs. The first section presents a division of average travel time very similar to Hensher (2001). The second section presents the arrival time with respect to a implied preferred arrival time very similar to Small et al. (1999) distribution of arrivals. The third section includes travel costs; a running cost is presented in addition to tolls costs. The second questionnaire is similar to the first questionnaire, except that the sections are not divided, and the distribution of arrival times is replaced with a row indicating the trip time variability (i.e. amount of minutes plus or less with respect to the travel time). Travel costs are presented as taxi fares, and toll costs. Li et al. (2010) tested the questionnaires with commuters and non-commuters, and found that non-commuters values less travel time savings, lateness penalties, and travel time reliability relative to commuters. The non-commuters’ reliability ratio is higher compared to commuters. In addition, Li et al. (2010) argued that the survey design similar to Small et al. (1999)’s first questionnaire is better understood by survey respondents in comparison to the survey design similar to Jackson and Jucker (1982)’s second questionnaire. It should be noted that there are differences between Li et al. (2010)’s second questionnaire and Jackson and Jucker (1982)’s questionnaire even though Li et al. (2010) considers them as similar. An important difference is that Jackson and Jucker (1982) presents variability as number of additional minutes of delay per week, and Li et al. (2010) presents delays by plus or less minutes with respect to the travel time.

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and logic the perception of respondents with regards to reliability presented in the questionnaires. Tseng et al. (2009) found that Small et al. (1999)'s format is preferred, and understood by most of the respondents. Copley et al. (2002)'s format showed signs of difficulty in understanding the probabilities from the graph by some of the respondents. Hollander (2006)'s format received mixed results. Tseng et al. (2009) recommends not using this format. In addition, Bates et al. (2001)'s format was not preferred compared to other formats by respondents.

In summary, stated preference studies have focused on exploring distinct presentations of variability to survey respondents based on mean-variance and scheduling approaches. Unfortunately, validation and testing whether survey respondents can understand the presentation has not received enough attention, except for early studies by Bates et al. (2001), Copley et al. (2002), Cook et al. (1999), and the recent pioneer study by Tseng et al. (2009). Most researchers agree that the variability presentation by Small et al. (1999) (which is in turn based on Black and Towliss (1993)) should be the current preferred presentation of travel time variability. It has been found it is understood by survey respondents, and it can be used to estimate both mean-variance and scheduling models. An alternative to Small et al. (1999)'s format is the histogram graphical representation (Copley et al. (2002), Tilahun and Levinson (2010)). This presentation seems to be understood by respondents, but an amount of effort is required to educate the respondents. Furthermore, there's still a need to test how subjects' preferences of travel time variability in stated choice experiments (abstract situations) compare to subjects' preferences in actual observed trips (see Louviere et al. (2000), Hensher (1994) and Hensher (2010) for discussions about SP vs. RP). Fig. 2 presents images of some of the discussed surveys.

1. Usual time: 50 minutes
   Possible delays: None
2. Usual time: 40 minutes
   Possible delays: 20 minutes once a week.

(a) Source: Jackson and Jucker (1982)

**EXPERIMENT #1 (SAMPLE QUESTION)**

<table>
<thead>
<tr>
<th>PLEASE CIRCLE EITHER CHOICE A OR CHOICE B</th>
</tr>
</thead>
<tbody>
<tr>
<td>Average Travel Time: 9 minutes</td>
</tr>
<tr>
<td>Average Travel Time: 6 minutes</td>
</tr>
<tr>
<td>You have an equal chance of arriving at any of the following times:</td>
</tr>
<tr>
<td>7 minutes early</td>
</tr>
<tr>
<td>4 minutes early</td>
</tr>
<tr>
<td>1 minute early</td>
</tr>
<tr>
<td>5 minutes late</td>
</tr>
<tr>
<td>9 minutes late</td>
</tr>
<tr>
<td>your cost: $0.25</td>
</tr>
</tbody>
</table>

(b) Source: Small et al. (1999)

(c) Source: Bates et al. (2001)

Fig. 2. Examples of SP experiments of travel time variability.
(a) Source: Hensher (2001)

(b) Source: Copley et al. (2002)

(c) Source: Hollander (2006)

Fig. 2 (continued)
(a) Source: Tilahun and Levinson (2010)

(b) SP Scenario with arrival distribution. Source: Li, Hensher and Rose (2010)

(c) SP scenario with explicit variability. Source: Li, Hensher and Rose (2010)
4.2. Revealed preference studies

There are few studies using revealed preference data investigating travel time reliability in the transportation literature. The main reasons for their scarcity are: few examples of experimental settings with significant contrast of travel time variation across at least two alternatives (e.g. high occupancy toll lanes); difficulties with measuring travel time data; costs associated with planning (e.g. methodology of experiment) and deployment (e.g. surveys, devices to measure travel time) of revealed preference studies; and others. In addition, revealed preference studies vary by the source of travel time measurements: objective travel time distribution (measured by devices such as loop detectors); and subjective travel time distribution (travel times reported by the subjects).

4.2.1. Objective travel time distribution

In Small (1982), revealed preference data of trip timing (i.e. individuals were asked about their arrival times, and work-start times) of commuters in the San Francisco Bay Area was fitted to the scheduling delay with choice model where the dependent variable were twelve intervals of time of 5 minutes. The travel-time data were obtained using a road network maintained by the Metropolitan Transportation Commission, and also it was supplemented by floating car observations. Small (1982) used this data to fit his proposed scheduling model (see Section 3.2). He found that travelers prefer early arrival, and additional travel time to late arrival, and prefer early arrival to addition travel time. In mathematical terms, the inequality $\gamma_2 > \gamma_1 > \gamma_3$ in Eq. (11). This relationship has been enforced in most (if not all) theoretical models considering cost functions (or utility functions) including early vs. late costs. This is especially seen in the bottleneck models mentioned earlier (e.g. Arnott et al. (1994)).

Most of the revealed preference research has been done by analyzing data collected from California State Route 91 (SR-91) in greater Los Angeles. A section of 10 miles of this freeway includes four untolled lanes, and two high occupancy toll lanes in each direction. The high occupancy toll lanes opened in 1995, and the tolls assigned to the lanes vary by time of day. In 1997 and 1998, Lam and Small (2001) collected revealed preference data through mail surveys from drivers identified in this corridor through their license plates. Travel-time data is collected from loop detectors. Lam and Small (2001) fits mean-variance approach for route choice models to the data. They did not use toll to represent travel costs, but rather use a proxy variable representing wage rate. They also estimate the models using distinct two measures of centrality (mean and median), and two measures of dispersion (standard deviation and 90th percentile minus median). In addition, they estimate route choice and time of day models. They consider the mean–variance (only the median and 90th percentile minus median) and scheduling approach for such models. Other models considered are route and mode choice, and transponder choice as well with similar approaches. They are able to estimate the value of travel time savings, and value of reliability, but they express doubt of these estimates as they are obtained through aggregated data (loop detectors) based on many assumptions. Small et al. (2005) and Small et al. (2006) collected both RP (actual preferences of subject’s lane choice) and SP (hypothetical scenarios to examine subject’s lane choice) observations, and consequently enriched their statistical model by pooling both types of data of SR-91 from 1999 to 2000. The collection consisted of three surveys: the first survey was a telephone interview of actual travel (revealed preference), and the other two were mail-back questionnaires (the first one about actual travel [revealed preference], and the other one about hypothetical scenarios [stated preference]). The set of actual alternatives was composed of High-Occupancy Toll lanes (HOT) and General Purpose Lanes (GPL). Commuters using the HOT lanes require an electronic transponder to pay a toll, which varies hourly. It should also be noted carpools (High Occupancy Vehicles (HOVs)) are allowed in the HOT lanes with a discount. The set of hypothetical alternatives remained the same as the actual with the exception of changing the values of variables such as time, cost and reliability. These changes allowed for the preferences of the subjects to be inferred based on their unique pattern of responses to trade-offs among the different hypothetical scenarios. The data was analyzed by a discrete-choice model; a utility function was specified containing attributes for the alternatives including toll, travel time and reliability. This statistical model approach allows for the estimation of the well known value of time (VOT), and the value of reliability (VOR). The latter value represents the susceptibility of the commuters to (un)reliability in monetary terms, and it is calculated as the ratio between the parameters of travel reliability and travel cost (toll cost in the study). This VOR represents the marginal rate of substitution between travel cost, and travel reliability. Right ranges (20th - 50th percentiles) of the travel time savings distribution (differences between travel time distributions of GPL and HOT) are used as (un)reliability measures. Another important feature of the model is the inclusion of a carpool variable in order to control for systematic bias. However, besides all these similarities the studies differ in certain key areas. The first study (Small et al., 2005) focuses solely in formulating a lane choice model (using mixed logit) by combining the RP and SP data. The results of the model indicate travel time and reliability to be significant, and that the heterogeneity in these factors is significant as well (thus implying the significance of the heterogeneity of VOT and VOR). In contrast, the second study (Small et al., 2006) models not only lane choice, but also vehicle occupancy and transponder acquisition. It also extends the previous study (Small et al., 2005) by using simulations to analyze distinct highway pricing policies besides the current one at CA-91. The policies simulated include: no toll, general purpose and HOV, general purpose and HOT, and combinations of the preceding cases. The objectives of these simulations is to point out the significance of the heterogeneous preferences of commuters to highway policymakers, and, as Small et al. points out, the current use of homogeneous preferences fails to account accurately for different policies working together. It should be noted that highway pricing policies are typically developed for congestion relief. The main notion being that congestion is a negative externality of the transportation system, and the use of pricing schemes will reduce any unnecessary trips, and persuade travelers to reconsider their
activity patterns in time and space. Readers may refer also to Yan (2002) for a very detailed account of Small et al. (2005) and Small et al. (2006). It should also be emphasized that the nature of the survey methods employed did not allow for some of the variables to be measured during each of the subject’s trips. For example, travel time was obtained by field measurements (performed by others instead of the subjects) corresponding approximately to the travel periods of the subjects. Thus, these measurements may have affected the accuracy of the data in the model. Lastly, Liu et al. (2004) also used data from SR-91, except that they used loop detector data. They propose an alternative method to RP and SP data. They consider aggregated counts from loop detectors, and origin-destinations from ramps along the freeways. Liu et al. (2004)’s VOT and VOT estimates are similar to those from the previous studies in the SR-91 freeway.

Another study in California is Ghosh (2001). The study uses data collected from the high occupancy toll (HOT) lanes in Interstate 15 in San Diego. In 1998, the tolls of the high occupancy toll lanes started being adjusted according to travel demand, and in order to maintain free flow traffic conditions. The tolls range were typically from USD$0.50 to USD$8.00 for single occupancy vehicles (i.e. solo drivers). High occupancy vehicles (i.e. carpoolers) continued to use the lanes without paying tolls. Ghosh (2001) used panel data collected by San Diego State University from 1998 to 1999. The panel consists of samples of HOT lane users (those that have transponders), other I-15 users, and users of I-8. He also used choice-based sampling to avoid over sampling HOT subscribers (transponder users). For travel time data, Ghosh (2001) asks subjects about the ramps they used to access the lanes, and uses traffic speeds from loop detector data, and estimates time savings based on arrival times from subjects. Moreover, Ghosh (2001) estimated mode choice models (choices where Subscriber, non-subscriber, carpooler, and others similar) using mean-variance approach. He considered for centrality measure the median, and for dispersion the 90th percentile minus the median. In addition, toll data was available to Ghosh (2001). In addition, stated preference data was collected in one of the panel waves asking simple questions whether a toll value and time saved will be acceptable to the subjects. However, the SP data was only used to estimate VOT as it did not have any connection with travel time variability. Therefore, only RP data is used to estimate value of reliability using mean-variance approach. Ghosh (2001) found estimates similar (but slightly higher) compared to the previously discussed California studies.

Another study using RP data is Bhat and Sardesai (2006). They collected revealed preference of mode choices from a web-based commuter survey in Austin, Texas. In addition, they designed a stated preference experiment where its attributes are pivoted from the revealed preference’s attributes. The travel time data is based on self reported travel times, but the travel time variability is only found in the stated preference experiment. They estimate mixed logit models using mean-variance approach (centrality: mean of travel time; dispersion: standard deviation). They estimated VOT and VOR estimates for SP model, and joint SP-RP models.

Another group of researchers also studied the high occupancy toll lanes, but in Interstate 394 at Minneapolis, Minnesota. Liu et al. (2007) uses loop detector data to estimate VOT and VOT based on the method of aggregate data discussed in Liu et al. (2004), but with variations to allow the estimates to be in function with time of day. They found that VOT and VOR values varied from about USD$5 to USD$30. A more recent study by Carrion and Levinson (2010) used Global Position System (GPS) devices and transponders, and proposed an experimental design to estimate VOT and VOR. Carrion and Levinson (2010) considered the route choice (untolled lanes, tolled lanes, and signalized arterials parallel to the I-394 corridor) of recruited subjects from the western suburbs, and with work locations near downtown Minneapolis. Each of the subjects was equipped with a GPS device and a transponder. Thus, subscription to the HOT lanes was not an issue. Succinctly, they proposed an experimental design where subjects will drive several weeks on each route alternative, and the last two weeks will be allowed to freely choose between the alternatives. The GPS devices allowed to ascertain the RP choices, and also the travel times and other related commute level data of the subjects. Surveys were also administered to collect socio-demographic data, and also to measure travelers preferences with regards to the alternatives. Unfortunately, the study suffered from high attrition due to the requirements of the experimental design, and also experience some data lost with regards to the GPS devices. Carrion and Levinson (2010) estimated mixed logit models using the mean-variance approach with different measures (centrality: mean, median; dispersion: standard deviation, 90th percentiles minus median, and interquartile range). The estimates of VOT and VOR were significantly lower (about USD$8) compared to the previous studies, but the estimates confidence intervals were wide enough to include the previous estimates of some of the other studies. In addition, Carrion and Levinson (2011) uses GPS data from another experiment by Zhu (2010). The GPS data was originally collected to study the travel behavior of commuters after the Interstate 35W bridge collapse in Minneapolis, Minnesota. Carrion and Levinson (2011) used this data to fits a bridge choice model where travelers chose the new I-35W bridge or any of the possible alternatives. They included variables such as mean travel time, and standard deviation of travel time for the alternatives, and thus also calculated reliability ratios, but not VOT and VOR estimates.

In summary, high occupancy toll (HOT) lanes of SR-91, I-15 in California, and I-394 in Minnesota have become the experimental settings for RP studies. A significant problem with the RP studies is the trade-off between measuring travel time data, and the cost associated with the devices to measure such data. Loop detector data is typically collected by many department of transportation in the US, and in many cases freely available to researchers. However, loop detector data may be difficult to adapt for statistical estimation as Lam and Small (2001) noted. Another approach followed by Small et al. (2005), Small et al. (2006), Yan (2002) consisted of driving on similar time periods as the subjects and measuring travel time. This approach may approximate the actual travel time the subjects experience when they revealed their choices. Lastly, GPS devices measure very detailed commute data, and also can be used to ascertain the revealed choices of the subjects. However, it is important to cautiously design methodologies that avoid the problems Carrion and Levinson (2010)
experienced. Furthermore, the mean-variance approach dominates the RP models (except for Lam and Small (2001)), because most likely preferred arrival times of the subjects were not collected.

4.2.2. Subjective travel time distribution

Up until this point, it has been assumed that travelers choose optimally under the objective travel time distribution (i.e. the perception error of travelers is close to zero). Bates et al. (2001) argues that it is likely travelers are optimizing according to their own divergent view of the objective distribution (i.e. based on actual measurements). Consequently, travelers will differ in their optimal solutions depending on the degree of distortion of their subjective distribution with regards to the objective distribution. This very likely as it has been shown in the transportation literature for different types of travel time such as waiting time (examples include Levinson et al. (2006), Levinson et al. (2004)). In this way, it is reasonable that the random variable representing subjective travel time \( T_s \) can be decomposed as: a random variable representing objective travel time \( T_o \), and a random perception error or distortion variable \( \Delta \). In other words, \( T_s = T_o + \Delta \). The probability density function of \( T_s \) can be obtained by solving a convolution integral (assuming independence) or, more general (assuming no independence), by solving the joint distribution integral (with its respective Jacobian of the transformation) as long as we know the probability density functions of \( T_o \) and \( \Delta \). Furthermore, the parameters of the probability density functions of \( T_o \) and \( \Delta \) could be estimated given the “proper” data. By “proper”, it refers to for example individual experienced travel time measurements in order to estimate the traveler's objective travel time distribution. In the case of the distortion distribution, the method is not so obvious.

Recently, Peer et al. (2010) studied the travelers' perception of their morning commute. Basically, they compared reported travel times by subjects from questionnaires, and compared them to their travel times from camera data. In essence, they compared reported travel time distributions (subjective) to camera travel time distributions (objective). They found that certainly perception error is an issue that need to be taken in consideration. This result should be emphasized as more RP studies may be underestimating or overestimating the value of time, and value of reliability as the objective travel time distributions differ to subjective travel time distributions. In other words, travelers may see worthwhile savings and predictability (low variability) that do not match the actual savings and predictability (low variability).

5. Meta-analysis

In other fields (mainly in social sciences), meta-analysis has been used to analyze and summarize the results of various studies. This method analyses data at a higher level; it searches for patterns in the results of other studies through statistical tools (e.g. meta-regression). Furthermore, these patterns (or differences) can be understood with the use of several regressors incorporating several key characteristics (e.g. regional variables) of each study. There are several advantages and disadvantages with meta-analysis that need to be taken in consideration. These are briefly discussed subsequently. Also, see Guzzo et al. (1987) and Arnqvist and Wooster (1995) for more details.

Several of the advantages of meta-analysis include:

- It identifies general patterns that may have been overlooked by conventional reviews.
- It provides objective evidence of the state of the research.
- It allows to control for between-study variations.
- Statistical power to detect an effect from the population of studies.

Several of the disadvantages of meta-analysis include:

- Many studies must be selected in order to reduce the bias of the authors for certain studies
- Ignoring the possible effects of study characteristics.

6. Data

A data set was assembled after an extensive search of studies with comparable estimates and methodology in transportation research journals, Google (scholar) search engine, and other articles' databases. Empirical studies were included according to the following criteria:

- Contained estimates of VOT, VOR, or RR that could be made comparable across studies;
- Stated explicitly and clearly how the expected travel time and travel time (un)reliability were measured;
- Sample size of the data was provided;

Table 1 presents the studies selected for the meta-analysis. Data Type refers to Stated Preference (SP), or Revealed Preference (RP) or both. Observations refers to the number of Reliability Ratio (RR) estimates available in each study, and the average of RR provides the mean among those observations. Maximum and Minimum values are included as well. Fig. 3 presents the reliability ratios found in the studies selected for the meta-analysis.
7. Methodology

The current differences among research in valuation of travel time reliability are a key problem in comparing estimates across studies. The main differences are classified by Tseng (2008) in:

- Data type (RP, SP, Joint RP and SP);
- Scheduling vs. reliability measures;
- Various travel time reliability measures (e.g. standard deviation, interquartile range);
- Travel time unit;
- Presence of heterogeneity (observed and unobserved);
- Choice dimensions (mode, route, transponder, and joint choices).

The data type differences (RP vs. SP) are mostly centered around perception issues for subjects, and multicollinearity of statistical estimates in econometric models. Succinctly, the validity of the preferences collected from SP data may be affected by the lack of realism, and the subject’s understanding of the abstract situations. Thus, the subject’s route preferences may not be similar to the ones during their actual trips (see Louviere et al. (2000) and Hensher (1994) for discussions about SP vs. RP). However, new modeling techniques (see Louviere et al., 2000) have been developed to combine RP and SP data, and to correct for the scale issues of one over the other. The idea behind these techniques is to ground stated choices (SP) to real choices, and to use SP data to stabilize RP data allowing to obtain more precise estimates. In terms of marginal rates of substitution (e.g. VOT, VOR, RR), distinct data types may provide estimates differing by order of magnitude. Generally, transportation researchers hypothesize that valuation ratios of SP estimates are smaller than RP estimates.

Reliability and Scheduling are related concepts. The former refers to the disutility because of the inconvenience and possible penalties attributed to the unreliability of travel times. The latter refers to the disutility of arriving either too early or...
too late, when the traveler has time restrictions (e.g. inflexible vs flexible schedules). These two may interact as travelers may have time restrictions and experience unreliable travel times, and thus obfuscate the contribution of each in the utility models estimates. This is important to remember as most of the valuation of travel time reliability studies have focused in commuters; a subset of travelers typically with time constraints. In other words, valuation ratios may depend on controlling for the contribution of both reliability and scheduling. However, most of the VOR studies have focused on using only reliability measures, and consequently not allowing this study to test for this in the meta-analysis.

There are three main distinctions among studies with regards to travel time. First, there are various measurements of travel time reliability in empirical studies including but not limited to: standard deviation, difference between 90th and 50th percentiles of travel time distribution, and others. Second, distinct travel time distributions have been used such as travel time of savings (difference between HOT Lanes and General Purpose Lanes’ travel time distributions; see Small et al. (2005)), and the actual travel time distribution of each (Carrion and Levinson, 2010). Third, travel time may depend on when it is evaluated during the day. The time of day has influence over the travel time. It is likely that measures from off-peak hours may differ from peak hours. In other words, valuation estimates may depend on the described effect. At the moment, most of the valuation of travel time reliability research has focused in the morning commute. A few including Carrion and Levinson (2010) have considered afternoon commute. In this study, these differences in travel time are referred as travel time unit. This lack of agreement generates difficulties for the comparison of empirical estimates across studies. Therefore, results of each valuation research must be examined by considering the assumptions of travel time distribution, reliability measures, and travel time unit.

Two types of heterogeneity can be included in the utility specification: observed and unobserved. The observed heterogeneity in the estimates can be evaluated by adding interaction terms of traveler attributes (e.g. age, gender) with travel time, reliability, or cost variables. In contrast, the unobserved heterogeneity (obtained by using mixed logit models) is evaluated by adding another stochastic term that allows to consider the individual units as draws from a population distribution. However, there are difficulties (especially for observed heterogeneity) in the calculation of valuation ratios, because the interaction terms enter in the marginal rate of substitution partial derivatives. This effect could be fixed by obtaining weighted means, but the more interaction terms included and lack of statistics (socio-demographics data) serves as additional obstacles. In the meta-analysis, observed heterogeneity is neglected. In contrast unobserved heterogeneity, it is included in the utility models through the use of advanced econometric modeling (mixed logit or multinomial probit). However, it is unclear whether unobserved heterogeneity leads underestimates or overestimates the valuation ratios. For example, Ghosh (2001) presented low estimates for the valuation ratios for his most general model, in contrast to his other models. Unobserved heterogeneity is considered in the meta-analysis.

Finally, the estimation of the marginal rates of substitution may be affected by distinct choice dimensions (e.g. route choice, mode choice). There might be differences in the choice behavior of travelers between mode and route (perhaps even departure time). In addition, these differences could also be attributed to the modeling (perhaps even endogeneity issues supporting joint choice models). In the meta-analysis, these difference of estimates are explored to identify the trend of the estimates with regards to these results. Furthermore, a procedure is outlined for making estimates comparable for the meta-regression in the correction of estimates section, and the variables of interest are covered along with the econometric model used in the meta regression section.

7.1. Correction of estimates

In discrete choice models (consistent with random utility theory), an utility function is specified and estimated, in order to obtain the marginal rate of substitution among distinct quantities of interest. In valuation of travel time reliability, the quantities of interest are measures of travel time, travel time reliability, and travel cost. However, the estimates of the utility function depends on the measures used for each variable. For example, a researcher could choose standard deviation (SD) as the (un)reliability measure, and another may choose the difference of the 90th and 50th percentiles (90D50). Assuming linear-additive in parameter function forms for both models, the utility functions are given in equations (5.5) and (5.6). It is trivial to notice that $\beta_d \neq \beta_r$, and thus the computed valuation ratios (VOR and RR) are different, because of measure rather than observations (samples). Furthermore, another difficulty is the travel time distribution used by the researcher (travel time of route vs. travel time savings) as it was mentioned in the previous section.

$$U = ASC + \beta_1 E(T) + \beta_2 SD + \cdots$$  \hspace{1cm} (18)

$$U' = ASC + \beta_1' E(T) + \beta_2' 90D50 + \cdots$$  \hspace{1cm} (19)

The best solution to both problems consists of using a standard methodology (i.e. same travel time distributions), and same (un)reliability measures on the same observations for each study. However, this requires reestimating, and performing transformations to the data sets. Unfortunately, these changes are not possible unless the data sets were available to the public (not necessarily a possibility as data sets can be costly). Other methods (as the ones outlined here) can be used to obtain reasonable solutions, although not necessarily better.

First, the different measure problem can be fixed by using “transformation ratios” (similar to Tseng (2008)). These ratios are obtained by normalizing for one measure to transform all measures to a common form (e.g. standard deviation). However, this requires an strong assumption on the shape of the travel time distribution. For example, the standard deviation...
(SD) and the difference of the 90th and 50th percentiles (90D50) can be obtained analytically or numerically for various theoretical distributions, and it can be normalized to transform one to the other or vice versa. In the case of travel time following an uniform distribution, the transformation ratio (0.723) of 90D50 to SD is obtained by taking the ratio of (5.8) to (5.7), where \( a \) and \( b \) are the parameters for an uniform distribution.

\[
90D50 = \frac{8}{20} (b - a)
\]

\[
SD = \frac{1}{2\sqrt{3}} (b - a)
\]

In this study, a normal distribution was selected for the transformation ratios because the distribution shape is hypothesized to be similar to the true distribution of travel times (statistical tests have indicated normal distributions as reasonable; see Zhu (2010)), it is tractable, and the transformation ratios are between uniform and triangle distributions (cases with no peak and peak travel times). The transformation ratios are grouped in Table 2.

In terms of travel time distribution differences, only three studies (Ghosh (2001), Yan (2002) and Small et al. (2005)) use the travel time savings approach. However, it can be noted that as the studies mention the HOT lanes are mostly operating at free flow conditions. Therefore, the travel times tend to be rather constant. This means that the travel time savings distribution is likely to resemble the GPL distribution but reduced by a constant for each value. It is trivial to show that if it is assumed that all values are reduced by a constant then the dispersion measures remain unaffected.

Other corrections with regards to travel cost unit (monetary value) are neglected, because in this meta-analysis only the reliability ratio is considered, and VOR and VOT are not analyzed. The main reason was to avoid including more confounding because of assumptions with respect to exchange rates, and the present value of capital.

7.2. Meta-regression

A meta-regression is a multivariate regression or any of its extension according to the required characteristics (e.g. heteroskedasticity, autocorrelation) of the data. Therefore it follows that a meta-regression is defined as

\[
y_n = \beta_0 + \beta_{1x} X_{1n} + \beta_{2x} X_{2n} + \beta_{3x} X_{3n} + \cdots + \beta_{kx} X_{kn} + \epsilon_n
\]

where \( y \) represents the reliability ratio (RR), \( x \) are the \( k \) regressors (outlined in subsequent paragraphs), \( \epsilon \) is the gaussian white noise (\( \epsilon \) i.i.d. \( N(0, \sigma^2) \)), and \( n \) are the number of observations.

The regressors are grouped into six classes. These are:

7.2.1. Unobserved heterogeneity

This is a categorical variable representing studies that included unobserved heterogeneity. This is a binary variable (denoted as Het), where 0 = did not include (base case), and 1 = included.

7.2.2. Travel time unit

This class contains two categorical variables representing the time of day the data was collected. These are: AM, and PM. The base case is PM.

7.2.3. Data type

This class contains three categorical variables representing the data type. These are: SP, RP and joint SP and RP. The base case is joint SP and RP.

7.2.4. Region

This class contains four categorical variables representing the regional differences. There are: Minnesota (MN), California (CA), Texas (TX), Spain (ESP), Australia (AU), Netherlands (ND), and United Kingdom (UK). The base case is Australia.

7.2.5. Year of study

This is a quantitative variable representing the trend of the estimates with regard to years of publication.

<table>
<thead>
<tr>
<th>Measure</th>
<th>Ratios</th>
</tr>
</thead>
<tbody>
<tr>
<td>Standard deviation</td>
<td>1.000</td>
</tr>
<tr>
<td>90th–50th Percentiles</td>
<td>0.780</td>
</tr>
<tr>
<td>80–50th Percentiles</td>
<td>1.188</td>
</tr>
<tr>
<td>75th–25 Percentiles</td>
<td>0.741</td>
</tr>
</tbody>
</table>
7.2.6. Choice dimension

This class contains three categorical variables representing the distinct choices. There are: mode choice, route, and joint choices (e.g. route choice + transponder choice). The base case is joint choices. The reader can refer to Wooldridge (2009) and Trivedi and Cameron (2005) for a complete review and additional information about these statistical (or econometric as there is overlap) models.

8. Results and discussion

Table 3 presents the results. There are three estimated models. All utilize the Reliability Ratio value as the dependent variable, and also the regressors as outlined in the previous section. First, a multivariate regression with Ordinary Least Squares (OLS) estimators was performed. However, most of the estimates turned out to not have statistical significance with the exception of a regional variable (Netherlands). A reason for this lack of statistical significance can be attributed to inefficient estimators (as standard errors enter in T-Statistics), because of heteroskedasticity. Therefore, a Breusch-Pagan test was performed and the homoskedasticity assumption of OLS was rejected at the 5% significance level. Therefore, a multivariate regression with OLS estimators and robust standard errors (RSTDE) was performed. This regression identified additional variables that did not have statistical significance for lack of OLS estimator efficiency.

The reliability ratio according to the OLS-RSTDE varies in size by the following statistical significant variables: region (CA).

It is prudent to look at all classes of regressors (even if they are not statistically significant) as there could be reasons or further insight into why they were not found “important” in describing the variation of the RR variable. The classes following previous order of appearance are:

8.1. Unobserved heterogeneity

The presence of unobserved heterogeneity was not found statistically significant. This is plausible as the RR estimates of models including it might not be as different as models without it. The differences are ameliorated by taking ratios of VOR to VOT (both estimates might reduce or increase by similar proportion). It is likely that meta-regressions for VOT or VOR could find this effect significant.

8.2. Travel time unit

The time of day when the data is collected was not found statistical significant. The results indicate that the RR value calculated in the morning is larger in comparison to the one in the afternoon. This agrees with Tilahun and Levinson (2009) and Liu et al. (2007). The former indicated different VOTs between the morning and afternoon commute. The afternoon commute presented the highest VOT. The latter estimated VOT and VOR as functions of time, and thus indicating that values reduce with time of day. The values were higher for regular peak hours. It should be noted that in order for RR to be higher either VOT reduces or VOR increases or both values increase by distinct proportions, but VOR must increase more.
8.3. Data type

The RR estimate seems unaffected by Data type (SP or RP or joint SP & RP). This result disagrees with mainstream opinion with regards to SP estimates vs. RP estimates. However, the reason for lack of statistical significance is probably attributed to both VOT and VOR estimates reducing in size by similar proportions rather than the optimistic idea of similarity of SP estimates to RP estimates. Ghosh (2001) and Yan (2002) find RP estimates to be of higher value (about twice) in comparison to SP estimates.

8.4. Region

The regional difference (only California) was found statistical significant. This is plausible as market conditions may differ regionally (and more by country). California (CA), Minnesota (MN), Spain (ESP), Netherlands (ND) and United Kingdom (UK) experienced higher RR estimates in comparison to the Australia studies. The magnitude of Netherlands and California were the highest. In the case of California, there are several reasons that can explain this, but a very likely one for California is congestion. Yan (2002)'s trip-based and person-based models of the SR-91’s congestion experiment (in LA, CA) agree with this statement.

It should be noted that individual study differences are captured by the regional variables.

8.5. Year of study

Most of the earlier studies used SP estimates, while the latter focused on RP estimates or joint SP & RP estimates. Therefore, this time trend needs to be further explored by increasing the sample of studies, and no final conclusions should be drawn.

8.6. Choice dimension

No choice dimension variable was found statistically significant. Thus indicating that users may value trade off between travel time reliability and travel time savings similar across choice dimensions. In principle, this is agreeable if the researchers utility specification adequately describes the travelers choice behavior, and thus there should not be much variation across choice dimensions.

9. Conclusion

In this study, the value of travel time reliability was reviewed along with the current approaches. The main theoretical approaches are: centrality-dispersion (or mean-variance) and scheduling models. The mean-variance is generally more common as it requires only knowledge of day-to-day travel time distributions unlike scheduling models that also require the knowledge of preferred arrival times (or the day-to-day distributions of arrival times). In addition, mean-variance models assume symmetric (i.e. equal) penalties for travel time variability (independent of the dispersion measure used). This assumption is strong especially for commuters that are arriving to their jobs. It is likely that they have asymmetrical penalties as lateness is less preferred compared to earliness. Thus, scheduling models should be preferred. In addition, the equivalence between mean-variance and scheduling models has been proved theoretically, and it has been observed empirically (lost of statistical significance when variables of both models are included in utility specifications). Moreover, the mean-variance approach is currently preferred to the scheduling models on practical grounds such as: the estimation of a value of reliability (instead of values of scheduling delay early and late); the estimation of a reliability ratio (VOR/VOT); and the ease of computing the required variables (centrality and dispersion measures) compared to scheduling models.

In stated preference studies, researchers have focus in the development of choice experiments with a variety of presentations of travel time variability. The objective is to find a presentation that matches the survey respondents understanding of the abstract situation with the analysts' intentions of the abstract situation. However, most researchers have not focused on validating such understanding, and it has become difficult to ascertain which estimates are more plausible than others (especially as there are few revealed preference studies). Fortunately, some of the early studies (Bates et al., 2001; Cook et al., 1999; Copley et al., 2002) have focused on testing whether qualitatively or quantitatively the survey respondents understanding of several proposed presentations. A recent pioneer study by Tseng et al. (2009) further studied this validation concern, and found that travelers are more capable of understanding with ease the Small et al. (1999)'s format (e.g. an average travel time, and a distribution of equally likely arrival times relative to an implied preferred arrival time; also both mean-variance and scheduling models may be estimated). Also, studies with histograms (Copley et al., 2002; Tilahun and Levinson, 2010) may be considered as well as long as survey respondents are educated with regards to what the histograms convey. Unfortunately, most of the research has ignored another important issue of how subjects’ preference of travel time variability in stated choice experiments compare to the subjects’ preferences in actual observed trips.

In revealed preference studies, the literature is dominated by data from high occupancy toll lanes, especially those of SR-91 in California. These lanes have become a experimental setting for reliability study as in some cases the contrast between
high occupancy toll lanes and parallel untolled lanes in terms of travel time savings and reliability is significant. The main problem with RP studies (besides the cost of planning and deployment of such studies) is the collection of usable travel time data of the subjects. Researchers have used loop detectors, in field measurements (driving on similar travel periods and the subjects), and GPS devices. The loop detectors require several assumptions (some questionable; see Lam and Small (2001)) and processing to estimate usable travel time data for the studies. In field measurements may be more usable and require less assumptions, but they do not reflect exactly the travel times experienced by the travelers. GPS devices measure very detailed commute level data of the travelers, but caution must be undertaken in methodological designs and possible requirements as attrition is a concern. In addition, the mean-variance dominates RP studies. This is possible as preferred arrival times were probably not collected, and mean-variance variables are less difficult to measure in comparison to variables required by scheduling models. Moreover, there’s an important gap between objective travel time (measured from devices) and subjective travel time (reported by subjects) that needs to be addressed. Subjects are likely to do their decisions based on their perceptions of travel times that should be connected to the objective distribution but with a distortion. A recent study by Peer et al. (2010) studied the travelers’ perception of their morning commute. Basically, they compared reported travel times by subjects from questionnaires, and compared them to their travel times from camera data. They found that certainly perception error is an issue that need to be taken in consideration. However, there are still no studies exploring such an important concern with regards to estimates of VOT and VOR.

Finally, a meta-analysis was performed using reliability ratios of several published studies. The results of the meta-regression is inconclusive, and more studies are probably required to disentangle any key differences.

Readers may also refer to other review treatments (as far as we know) of value of reliability are Noland and Polak (2002), Small and Verhoef (2007, Chapter 2, pp. 52–54), Li et al. (2010) and Nakayama (2010).

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References


